

SUBJECT : STATISTICS

Probability : Random experiment, sample space, event algebra of events, probability on a discrete sample space, basic theorems of probability and simple examples based thereon the conditional probability of an event, independent events, Bayes theorems and its application, discrete and continuous random variables and their distributions, expectation moments, moment generating function, joint distribution of two or more random variables, marginal and conditional distributions, independence of random variables, covariance, correlation coefficient, distribution of a function of random variables, Bernoulli binomial, geometric negative binomial, by hypergeometric, poisson, multinomial, uniform, beta exponential, gamma Cauchy, normal, lognormal and bivariate normal distributions, real -life situations where these distributions provide appropriate models, Chebyshev's inequality, weak law of large numbers and central limit theorem for independent and identically distributed random variables with finite variance and their simple applications.

Statistical methods : Concept of a statistical population and a sample, types of data presentation and summarization of data , measures of central tendency, dispersion, skewness and kurtosis measures of association and contingency, correlation, rank correlation, interclass correlation, correlation ratio simple and multiple linear regression, multiple and partial correlations (involving three variables only) Curve fitting and principle of least squares, concepts of random sample, parameter and statistic, χ^2 , t and F statistics and their properties and applications, distributions of sample range and median (for continuous distributions only), censored sampling (concept and illustrations).

Statistical Inference : Unbiasedness, consistency efficiency, sufficiency, completeness , minimum variance unbiased estimation, Rao Blackwell theorem, Lehmann-Scheffe theorem, Cramer-Rao inequality and minimum variance bound estimator, moments, maximum likelihood, least squares and minimum chi-square, methods of estimation, properties of maximum likelihood and other estimators, idea of a random interval, confidence intervals for the parameters of standard distributions, shortest confidence intervals, large sample confidence intervals.

Simple and Composite hypotheses, two kinds of errors, level of significance, size and power of a test, desirable properties of a good test, most powerful test, Neyman-pearson lemma and its use in simple examples, uniformly most powerful test likelihood ratio test and its properties and applications.

Chi-Square test, sign test Wald-Wolfowitz runs test, run test for randomness, median test, Wilcoxon-Mann-Whitney test.

Wald's sequential probability ratio test, OC and ASN functions, application to binomial and normal distributions.

Loss function, risk function, minimax and Bayes rules.

Sampling Theory and Design of Experiments : Complete enumeration Vs. Sampling, need for sampling, basic concepts in sampling, designing large scale sample surveys, sampling and non sampling errors, simple random sampling, properties of a good estimator, estimation of sample size, stratified random sampling, systematic sampling, cluster sampling, ratio and regression methods of estimation under simple and stratified random sampling, double sampling for ratio and regression methods of estimation, two stage sampling with equal size first-stage units.

Analysis of variance with equal number of observation per cell in one, two and three way classifications, analysis of covariance in one and two way classifications, basic principles of experimental designs, missing plot technique 2^k factorial design, total and partial confounding 3_2 factorial experiments, split-plot design and balanced incomplete block design.